Impact of Interference Cancellation Technique on Throughput of Nonorthogonal CSK/SSMA ALOHA System

Nobuyoshi KOMURO, Member, IEEE, and Hiromasa HABUCHI, Member, IEEE

Abstract—The nonorthogonal Code Shift Keying (CSK)/SSMA ALOHA system was proposed in order to improve DS/SSMA ALOHA system performance. Its throughput improves with the length of the nonorthogonal signals. However, it is not efficient for each user to have exceedingly-long signals in a wireless network with finite population. Introducing interference cancellation into our system is expected to raise system performance without increasing signal length. This paper presents a theoretical analysis of the throughput performance of nonorthogonal CSK/SSMA ALOHA system with an interference canceler. The results show that the throughput performance of the nonorthogonal CSK/SSMA ALOHA can exceed 1.0 with the interference canceler. It is also found that the throughput of this system exceeds that of DS/SSMA ALOHA system.

Index Terms—Code Shift Keying (CSK), Nonorthogonal signal, ALOHA, Interference Canceler, maximum throughput

I. INTRODUCTION

The advanced wireless networks, such as Wireless Personal Area Networks (WPANs) are attracting more interest [1]-[4]. The Direct Sequence Spread Spectrum Multiple Access (DS/SSMA) ALOHA system is widely used in such wireless networks because of its two key advantages; simple transmission procedure and multiple access [5] and [6].

In [7]-[12], multiple-access-interference cancellation techniques are studied for achieving high throughput. The nonorthogonal Code Shift Keying/Spread Spectrum Multiple Access (CSK/SSMA) ALOHA system, which is one of the code-multilevel modulations, is proposed for improving the throughput performance of the DS/SSMA ALOHA system [13] and [14].

In [13] and [14], it is showed that the throughput performance of the nonorthogonal CSK/SSMA ALOHA system is better than that of the conventional DS/SSMA ALOHA system. It is also showed that the throughput of the system in [13] and [14] improves as nonorthogonal signal length is increased. Unfortunately, achieving high throughput needs exceedingly long signals. Such signals are not efficient in small-sized wireless networks. It is expected that the introduction of interference cancellation in order to overcome this issue [7].

Introducing an interference canceler into the nonorthogonal CSK/SSMA ALOHA system is expected to improve the spectral efficiency and the throughput. The effect of interference cancellation on DS/SSMA ALOHA system has been investigated [8] and [9]. Some papers [11] and [12] study the cancellation algorithm for enhancing the interference cancellation capabilities. Combination of the cancellation technique and the other technique for achieving high throughput is not really studied. The effect of the interference cancellation on the nonorthogonal CSK/SSMA ALOHA system is unclear. Its effect is expected to be great because the code-multilevel modulations and the interference canceler go well together.

In this paper, the authors derive the throughput of the nonorthogonal CSK/SSMA ALOHA system theoretically, and then evaluate its throughput. The authors investigate the improvement in throughput made possible by adding interference cancellation. The authors compare it to two conventional SSMA ALOHA systems: the DS/SSMA ALOHA system and the orthogonal CSK/SSMA ALOHA system. The outline of this paper is as follows. Section 2 details the model of our system. Section 3 analyzes its throughput performance. Section 4 describes its measured throughput performance. Section 5 summarizes the main results.

II. SYSTEM MODEL

A. Network model

Figure 1 shows the model of our system. In order to distinguish users, each user has a unique Pseudo-Noise (PN) code. All users have the same $M_{\text{non}}$ nonorthogonal signals, $(C_1, C_2, \ldots, C_{M_{\text{non}}})$, which are used for CSK.

The notation used in the following discussion is shown in Table 1.
TABLE I

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>(L_{p\text{-info}})</td>
<td>Number of bits of a packet [bit]</td>
</tr>
<tr>
<td>(L_p)</td>
<td>Packet length [signals]</td>
</tr>
<tr>
<td>(L_{\text{signal}})</td>
<td>Signal length</td>
</tr>
<tr>
<td>(M_{\text{os}})</td>
<td>Number of orthogonal codes</td>
</tr>
<tr>
<td>(M_{\text{con}})</td>
<td>Number of concatenations</td>
</tr>
<tr>
<td>(M_{\text{non}})</td>
<td>Number of nonorthogonal signals</td>
</tr>
<tr>
<td>(N_{\text{bit}})</td>
<td>Number of bits per nonorthogonal signal (=(\log_2 M_{\text{os}}+M_{\text{con}}))</td>
</tr>
<tr>
<td>(K)</td>
<td>Number of users</td>
</tr>
<tr>
<td>(k)</td>
<td>Number of interfering packets</td>
</tr>
<tr>
<td>(G)</td>
<td>Average number of generated packets in a packet duration (Offered Load)</td>
</tr>
</tbody>
</table>

### B. Transmitter

When transmitting, the transmitter carries out the following procedures:

1. The information carried by the packet, \(L_{p\text{-info}}\), is divided into \(L_{\text{p-info}} \div N_{\text{os}} \) bits.
2. One of \(M_{\text{non}}\) nonorthogonal signals is selected.
3. The selected nonorthogonal signal is multiplied by the assigned PN code. Each nonorthogonal signal has the same length and the same chip interval as the PN code.
4. One packet, which consists of \(L_p\) signals, is multiplied by the carrier, and the result is transmitted.

### C. Nonorthogonal signals

Figure 2 shows an example of nonorthogonal signals. In our system, nonorthogonal signals are constructed systematically. One nonorthogonal signal is constructed by concatenating 3 orthogonal codes, which we call primitive orthogonal codes. The nonorthogonal signals are constructed by concatenating with following patterns: \((0,0,0), (0,0,1), (0,1,0), (0,1,1), (1,0,0), (1,0,1), (1,1,0),\) and \((1,1,1)\). One primitive orthogonal codes constructs \(8 (=2^3)\) nonorthogonal signals. The group of nonorthogonal signals constructed from orthogonal code \(#i\) is called group \(#i\). The signals are orthogonal among the groups, but nonorthogonal in the same group.

### D. Cross correlation value

Table II shows the cross-correlation values of the nonorthogonal CSK/SSMA system when \(M_{\text{os}}=64, M_{\text{con}}=3\).

The correlation values, which are normalized to the number of CSK signals, are \(\{1, 1/3, 0, -1/3, -1\}\), and the number of signals, whose correlation values are 0, is \(8M_{\text{os}}-1\). The correlation values of the orthogonal CSK/SSMA ALOHA system are \(\{1, 0\}\), and the number of signals, whose correlation values are 0, is \(M_{\text{os}}-1\).

![Fig. 1. System model](image1)

![Fig. 2. Structure of nonorthogonal signal](image2)

![TABLE II

<table>
<thead>
<tr>
<th>System</th>
<th>Correlation value</th>
<th>Num. of seq.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nonorthogonal</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>CSK/SSMA</td>
<td>1/3</td>
<td>3</td>
</tr>
<tr>
<td>(M_{\text{con}}=3)</td>
<td>0</td>
<td>8(M_{\text{os}}-1)</td>
</tr>
<tr>
<td></td>
<td>-1/3</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>-1</td>
<td>1</td>
</tr>
<tr>
<td>Orthogonal</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>CSK/SSMA</td>
<td>0</td>
<td>(M_{\text{os}}-1)</td>
</tr>
</tbody>
</table>
E. Receiver with interference canceler

Figure 3 shows the canceler of our system. All transmissions are assumed to be synchronized completely, and each time delay adjustment is perfect. The receiver carries out the following procedures:
1. The received signal is multiplied by each PN code.
2. The signal is correlated with CSK signals and then re-modulated with the same signal.
3. The re-modulated signal is re-spread by the same PN code again in order to re-construct the interfering packets.
4. The re-spread signal is subtracted from the original received signal. Subtraction is done for each signal.
5. The subtraction result is demodulated for each signal.
6. $N_{bit}$ [bit] data is demodulated by estimating the transmitted primitive orthogonal sequence and the concatenating pattern.

III. THEORETICAL ANALYSIS

A. Assumptions

The authors assume the following when analyzing the throughput performance. Notations used in the analysis are written in Table III.

- Every transmitted signal is received by the central station with equal power: i.e. transmitted signal power is controlled by the central station.
- The number of bits per packet is fixed at $L_{p-info}$ bits. When the duration of a nonorthogonal signal is $\Delta t$, packet duration, $T_p$, is

$$T_p = \frac{L_{p-info}}{N_{bit}} \Delta t = L_p \Delta t.$$  

- The offered load, SG, is defined as the average number of generated packets in $T_p$. $G_{chip}$ is defined as the offered load in the chip interval:

$$G_{chip} = \frac{G}{L_p M_{con} M_{ox}} = \frac{G}{L_p L_{signal}}.$$  

The authors assume that each signal has the same length as its PN code.
- The number of users is finite. Packet generation follows a binomial distribution.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Pe(k)$</td>
<td>Error rate of a nonorthogonal signal when the number of interfering packets is $k$</td>
</tr>
<tr>
<td>$SNR(z)$</td>
<td>Signal to noise ratio when the interfering energy is $z$</td>
</tr>
<tr>
<td>$P_{occ}(z)$</td>
<td>Probability that a primitive orthogonal code is estimated successfully when the number of interfering packets is $k$</td>
</tr>
<tr>
<td>$ke_1$</td>
<td>Number of interfering packets after re-modulation</td>
</tr>
<tr>
<td>$ke_2$</td>
<td>Number of interfering packets for the primitive orthogonal code</td>
</tr>
<tr>
<td>$Pc(k)$</td>
<td>Probability that a nonorthogonal signal is received successfully when the number of interfering packets is $k$</td>
</tr>
<tr>
<td>$Ps(k)$</td>
<td>Probability that one packet is received successfully when the number of interfering packets is $k$</td>
</tr>
</tbody>
</table>

B. Frame success rate

If a signal error occurs, the incorrect signal is subtracted from the desired signal. In our system, each signal is constructed by concatenating primitive orthogonal codes. Cancellation error occurs in two ways:

- Primitive orthogonal code is estimated incorrectly. Then, the power of the interfering signal is doubled. (Error pattern 1)
- Primitive orthogonal code is estimated correctly but its polar characteristics are estimated incorrectly. That is, the power of the interfering signal is quadrupled. (Error pattern 2)

We assume that signal to noise ratio (SNR) at the receiver fluctuates according to Gaussian distribution. When the number of interfering packets is $SkS$, error rate of one signal for error pattern 1, $Pe(ke)$, is given by
\[ Pe(k_2) = \int_{k_2-2\sigma_j}^{k_2+2\sigma_j} \frac{1}{\sqrt{2\pi\sigma_j^2}} \exp \left( -\frac{(z-k_2)^2}{2\sigma_j^2} \right) \]

where \( k_2 \) is the number of interfering packets after re-modulation,

\[ k_2 = 2k(1 - P_{oc}(k)). \]  

(2)

\[ SNR(z) = \frac{1}{2} \left[ \frac{|z|}{3L_{signal}} + \frac{1}{2} \left( \frac{N_0}{2N_{ba}E_b} \right) \right]^{-1}. \]

(3)

\[ P_{oc}(z) = \int_{-\infty}^{\infty} f(x_i) \left[ \int_{-\infty}^{t_i} f(X_j) dx_j \right]^{M_{con}-1} dx_i. \]

(4)

\[ f(x_i) = g(|q_j|) \otimes \cdots \otimes g(|q_j|), \]

(5)

\[ g(q_j) = \frac{1}{\sqrt{2\pi\sigma_j^2}} \exp \left[ -\frac{1}{2} \left( \frac{q_j - \mu_j}{\sigma_j} \right)^2 \right]. \]

(6)

In this section, the authors show the throughput performance and the maximum throughput of our system. From [14], the authors found that the optimum number of concatenations is 4 in our system with access control. Thus, the authors set the number of concatenations \( M_{con} \) to 4. The authors compare our system with the conventional systems. In the comparison, the number of bits per packet is fixed, thus the packet length differs by systems; our system, the orthogonal CSK/SSMA ALOHA system and the DS/SSMA ALOHA system.

A. Throughput of our system

Figure 4 shows the throughput of our system for the number of bits per packet, \( L_{bit} = 2520 \) [bit], the number of users, \( K = 200 \), the number of primitive orthogonal codes, \( M_{os} = 32 \), the number of concatenations, \( M_{con} = 4 \), the signal length, \( L_{signal} = 128 \), the packet length, \( L_p = 280 \) [signals], and \( E_b/N_0 = \infty \) [dB]. The vertical axis represents the normalized throughput [bits/chip], and the horizontal axis represents the offered load in [dB]. The throughput improves by introducing the interference cancellation technique. The maximum throughput of nonorthogonal CSK/SSMA ALOHA with the interference canceler is 3.5 times better than that without the interference canceler.

Figure 5 shows the maximum throughput of our system versus the number of concatenations, \( M_{con} \). The vertical axis represents the maximum throughput, and the horizontal axis represents \( M_{con} \). In this figure, \( (M_{os}, M_{con}) = (128, 1), (64, 2), (32, 4), (16, 1) \). There is an optimum number of concatenations, \( M_{con} \). The reason why the optimum number exists is the trade-off between the effect of inter-symbol-interference and the increase of data-transmission rate per symbol. The throughput for \( M_{con} = 4 \) is the highest in the nonorthogonal CSK/SSMA ALOHA system. The following throughput evaluations consider \( M_{con} = 4 \).
**B. Throughput comparison**

Figure 6 shows the normalized throughput versus $G_{\text{chip}}$ when $K=200$, $L_{p-\text{info}}=2520$ [bit], and $E_b/N_0=\infty$ [dB]. In the nonorthogonal CSK/SSMA ALOHA system, $M_{os}=32$, $M_{con}=4$, $L_{signal}=128$, and $L_p=280$. In the orthogonal CSK/SSMA ALOHA system, $L_{signal}=M_{os}=128$ and $L_p=360$. In the DS/SSMA ALOHA system, $L_{signal}=128$ and $L_p=2520$. Nonorthogonal CSK/SSMA ALOHA has 1.02 times higher maximum throughput than orthogonal CSK/SSMA ALOHA, and 1.29 times higher maximum throughput than DS/SSMA ALOHA. From Fig. 6, the maximum throughputs of the nonorthogonal CSK/SSMA ALOHA system exceed 1.0 due to the advantage of multilevel modulation.

Figure 7 shows the maximum throughput versus $E_b/N_0$ for $K=200$, $L_{p-\text{info}}=2520$ [bit]. In the nonorthogonal CSK/SSMA ALOHA system, $M_{os}=32$, $M_{con}=4$, and $L_p=280$. $M_{os}=128$ and $L_p=360$ in the orthogonal CSK/SSMA ALOHA system. $L_p=2520$ in the DS/SSMA ALOHA system. Figure 8 shows that the throughput performance of our system does not improve so much in noisy channels ($E_b/N_0$ is low). This is because some incorrect signals may be subtracted from the signal received over noisy channels. The authors also found that the nonorthogonal CSK/SSMA ALOHA with the interference canceler offers the highest maximum throughput. Moreover, the CSK/SSMA ALOHA systems have throughputs of over 1.0 while DS/SSMA does not exceed 1.0.

Figure 8 shows the throughput versus the offered load for $\sigma^2=0.25$, 1.0, and 4.0 when $K=200$, $L_{p-\text{info}}=2520$ [bit], $L_{signal}=128$, $M_{os}=32$, and $M_{con}=4$. Figure 9 shows the maximum throughputs of the nonorthogonal CSK/SSMA ALOHA system, the orthogonal CSK/SSMA ALOHA system and the DS/SSMA ALOHA system versus $\sigma^2$. The throughput performance degrades when the influence of cancellation-error increases. Especially, the CSK/SSMA ALOHA systems affect the influence of cancellation-error compared with the DS/SSMA ALOHA system. The throughput of the CSK/SSMA ALOHA system, however, is better than that of the DS/SSMA ALOHA system.
This paper presents the evaluation of throughput performance of the nonorthogonal CSK/SSMA ALOHA with an interference cancellation technique. In the nonorthogonal CSK/SSMA ALOHA, the nonorthogonal sequences which are used for CSK are constructed by concatenating $M_{\text{con}}$ primitive orthogonal sequences. Our study indicated that introducing an interference cancellation technique into the nonorthogonal CSK/SSMA ALOHA is very effective. From the numerical results, we obtained the following points:

- The normalized throughput (maximum throughput) can exceed 1.0. The nonorthogonal CSK is one of the multilevel modulation systems, and it has the usual effect of $M$-ary/SSMA. So, some bits can be demodulated successfully at the same time. Moreover, the spectral efficiency of our system can exceed 1.0 as well as that of M-ary/SSMA [7].

- The throughput performance of our system shows about 3.5 times increase by using the interference cancellation technique.

- When comparing the nonorthogonal CSK/SSMA ALOHA system with the conventional SSMA ALOHA systems, the maximum throughput of nonorthogonal CSK/SSMA ALOHA system with the interference canceler is the highest.

From above, we can conclude that the nonorthogonal CSK/SSMA ALOHA with the interference canceler is effective.

Future works include investigating the impact of the interference cancellation technique on nonorthogonal CSK/SSMA ALOHA under fading channels, finding a way to reduce the signal error, evaluating the proposed system by simulation, the implementation of successive interference

V. CONCLUSION
canceller, and investigating the nonorthogonal CSK/SSMA system that uses access control together with the interference cancellation.

REFERENCES


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